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Futures, Scheduling and Work Distribution

Proseminar Nebenläufige Programmierung

Sommersemester 2010





Um was geht es?

- Programme Aufteilen und parallel ausführen
- Effizienz und Parallelität analysieren
- Thread Management



Themen

- Parallel Programming
- Analyzing Parallelism
- Realistic Multiprocessor Scheduling
- Work Distribution
- Work-Stealing DEQueues
- Work Balancing



Parallele Programme

- Typische parallele Probleme
 - Server Anfragen; Producer & Consumer; Brute-Force-Suche
- Nicht so offensichtlich parallele Probleme
 - Matrizenmultiplikation



Matrizenmultiplikation

$$C_{ij} = \sum_{k=0}^{N-1} a_{ik} * b_{kj}$$

$$C_{00} = 1*2 + 3*4 = 14 \quad C_{01} = 2*0 + 3*2 = 6$$

$$C_{10} = 1*1 + 1*4 = 5 \quad C_{11} = 1*0 + 1*2 = 2$$

		B:	1	0
A:		C:	4	2
2	3		14	6
1	1		5	2



Matrizenmultiplikation

```
class MMThread {
    double[][] a, b, c;
    int n;
    public MMThread(double[][] a, double[][] b) {
        n = a.length;
        this.a = a;
        this.b = b;
        this.c = new double[n][n];
    }
    void multiply() {
        Worker[][] worker = new Worker[n][n];

        for (int row = 0; row < n; row++)
            for (int col = 0; col < n; col++)
                worker[row][col] = new Worker(row, col);

        for (int row = 0; row < n; row++)
            for (int col = 0; col < n; col++)
                worker[row][col].start();

        for (int row = 0; row < n; row++)
            for (int col = 0; col < n; col++)
                worker[row][col].join();
    }
}
```

```
class Worker extends Thread {
    int row, col;
    Worker(int row, int col) {
        this.row = row; this.col = col;
    }
    public void run() {
        double dotProduct = 0.0;
        for (int i = 0; i < n; i++) {
            dotProduct += a[row][i] * b[i][col];
        }
        c[row][col] = dotProduct;
    }
}
```



Matrizenmultiplikation

- Probleme?
 - Was passiert bei 1000 X 1000 Matrizen?
→ Extremer Verwaltungs-Overhead
- Lösung:
 - Thread-Pools
 - Threads werden wiederverwendet



Futures und Thread-Pools in Java

- Interface: `java.util.concurrent.ExecutorService`

```
Future<?> future = executor.submit(Runnable task);  
future.get(); //nur Warten
```

```
Future<T> future = submit(Callable<T> task);  
T value = future.get(); //Warten auf ein Ergebnis
```

- Achtung Parallele Ausführung ohne Gewähr!



Matrizenaddition

- Zur Vereinfachung $A(n \times n)$: $n = 2i$ ($i \in \mathbb{N}$)
- $C = A + B$

$$\begin{pmatrix} C_{00} & C_{01} \\ C_{10} & C_{11} \end{pmatrix} = \begin{pmatrix} A_{00} + B_{00} & B_{01} + A_{01} \\ A_{10} + B_{10} & A_{11} + B_{11} \end{pmatrix}$$



Matrizenaddition

```
private static class Matrix {
    int dim;
    double[][] data;
    int rowDisplace;
    int colDisplace;
    Matrix(int d) {
        dim = d;
        rowDisplace = colDisplace = 0;
        data = new double[d][d];
    }
    Matrix(double[][] matrix, int x, int y, int d) {
        data = matrix;
        rowDisplace = x;
        colDisplace = y;
        dim = d;
    }
    double get(int row, int col) {
        return data[row+rowDisplace][col+colDisplace];
    }
    void set(int row, int col, double value) {
        data[row+rowDisplace][col+colDisplace] = value;
    }
    int getDim() {
        return dim;
    }
}
```

```
Matrix[][] split() {
    Matrix[][] result = new Matrix[2][2];
    int newDim = dim / 2;
    result[0][0] = new Matrix(data,
        rowDisplace, colDisplace, newDim);
    result[0][1] = new Matrix(data,
        rowDisplace, colDisplace + newDim, newDim);
    result[1][0] = new Matrix(data, rowDisplace
        + newDim, colDisplace, newDim);
    result[1][1] = new Matrix(data, rowDisplace
        + newDim, colDisplace + newDim, newDim);
    return result;
}
```



```
public class MatrixTask {
    static ExecutorService exec = Executors.newCachedThreadPool();
    ...
    static Matrix add(Matrix a, Matrix b) throws InterruptedException, ExecutionException {
        int n = a.getDim();
        Matrix c = new Matrix(n);
        Future<?> future = exec.submit(new AddTask(a, b, c));
        future.get();
        return c;
    }
    static class AddTask implements Runnable {
        Matrix a, b, c;
        public AddTask(Matrix a, Matrix b, Matrix c) {
            this.a = a; this.b = b; this.c = c;
        }
        public void run() {
            int n = a.getDim();
            if (n == 1) {c.set(0, 0, a.get(0,0) + b.get(0,0));} else {
                Matrix[][] aa = a.split(), bb = b.split(), cc = c.split();
                Future<?>[][] future = (Future<?>[][]) new Future[2][2];
                for (int i = 0; i < 2; i++)
                    for (int j = 0; j < 2; j++)
                        future[i][j] = exec.submit(new AddTask(aa[i][j], bb[i][j], cc[i][j]));
                for (int i = 0; i < 2; i++)
                    for (int j = 0; j < 2; j++)
                        future[i][j].get();
            }
        }
    }
}
```



Fibonacci-Folge

$$F(n) \begin{cases} 1 & \text{if } n = 0 \text{ or } 1 \\ F(n-1) + F(n-2) & \text{if } n > 1 \end{cases}$$

$$F(4) =$$

$$F(3) = \quad + \quad F(2) =$$

$$F(2) = \quad + \quad F(1) \quad F(1) + F(0)$$

$$F(1) + F(0)$$

Paralleles Potential da, aber auch Abhängigkeiten!



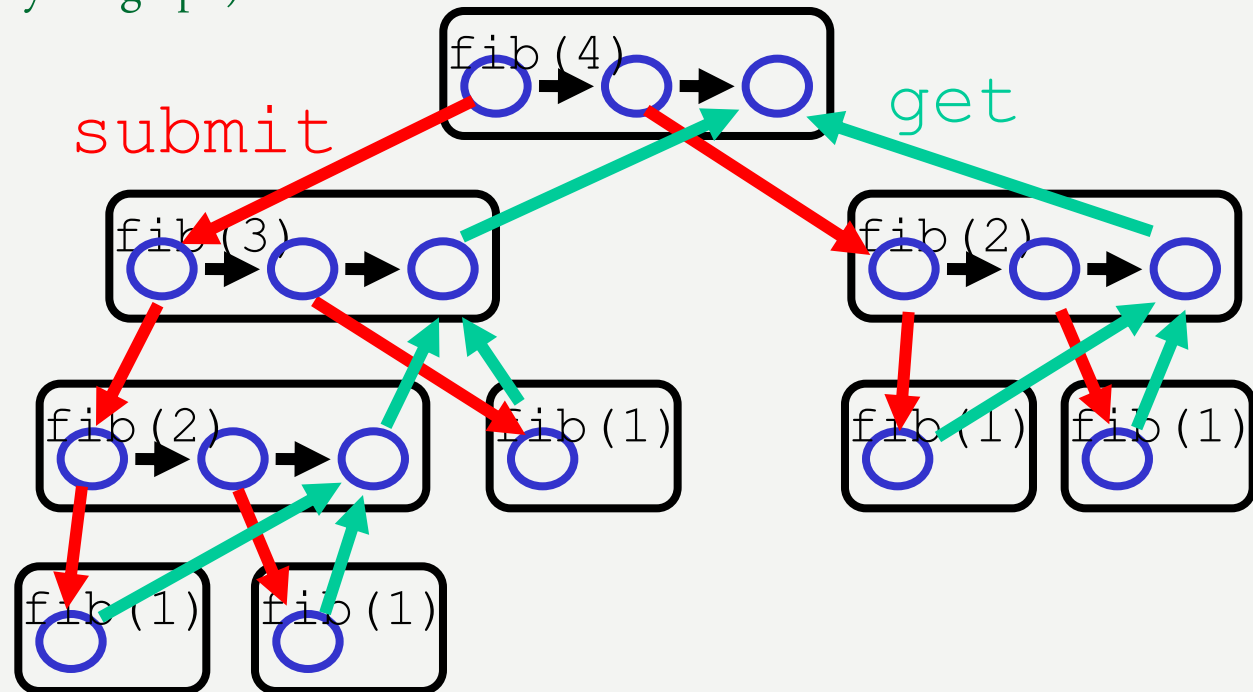
Multithreaded Fibonacci

```
•class FibTask implements Callable<Integer> {  
  
    static ExecutorService exec = Executors.newCachedThreadPool();  
    int arg;  
    public FibTask(int n) {  
        arg = n;  
    }  
    public Integer call() {  
        if (arg > 2) {  
            Future<Integer> left = exec.submit(new FibTask(arg-1));  
            Future<Integer> right = exec.submit(new FibTask(arg-2));  
            return left.get() + right.get();  
        } else {  
            return 1;  
        }  
    }  
}
```



Dynamisches Verhalten analysieren

- DAG (directed acyclic graph)





Dynamisches Verhalten analysieren

- T_p = Sequentielle Anzahl von Rechenschritten auf p Prozessoren
- T_1 = Rechenschritte auf einem Prozessor
 - $T_p \geq T_1/p$
- T_∞ = Rechenzeit auf ∞ Prozessoren
 - T_1/T_p = speedup auf p Prozessoren
 - T_1/T_∞ = max speedup, Parallelität einer Berechnung



Dynamisches Verhalten analysieren

- Matrizenaddition

 - Besteht rekursiv aus 4 Additionen + split

- $A_p(n)$

$$A_1(n) = 4A_1(n/2) + \Theta(1) = \Theta(n^2)$$

$$A_\infty(n) = A_\infty(n/2) + \Theta(1) = \Theta(\log n)$$

- Parallelität

$$A_1(n)/A_\infty(n) = \Theta(n^2)/\Theta(\log n)$$

$$n=1000; 10^7 / \sim 10 = 10^6$$



Dynamisches Verhalten analysieren

- Achtung: Hohe Parallelität != Hohe Performanz
- Warum?



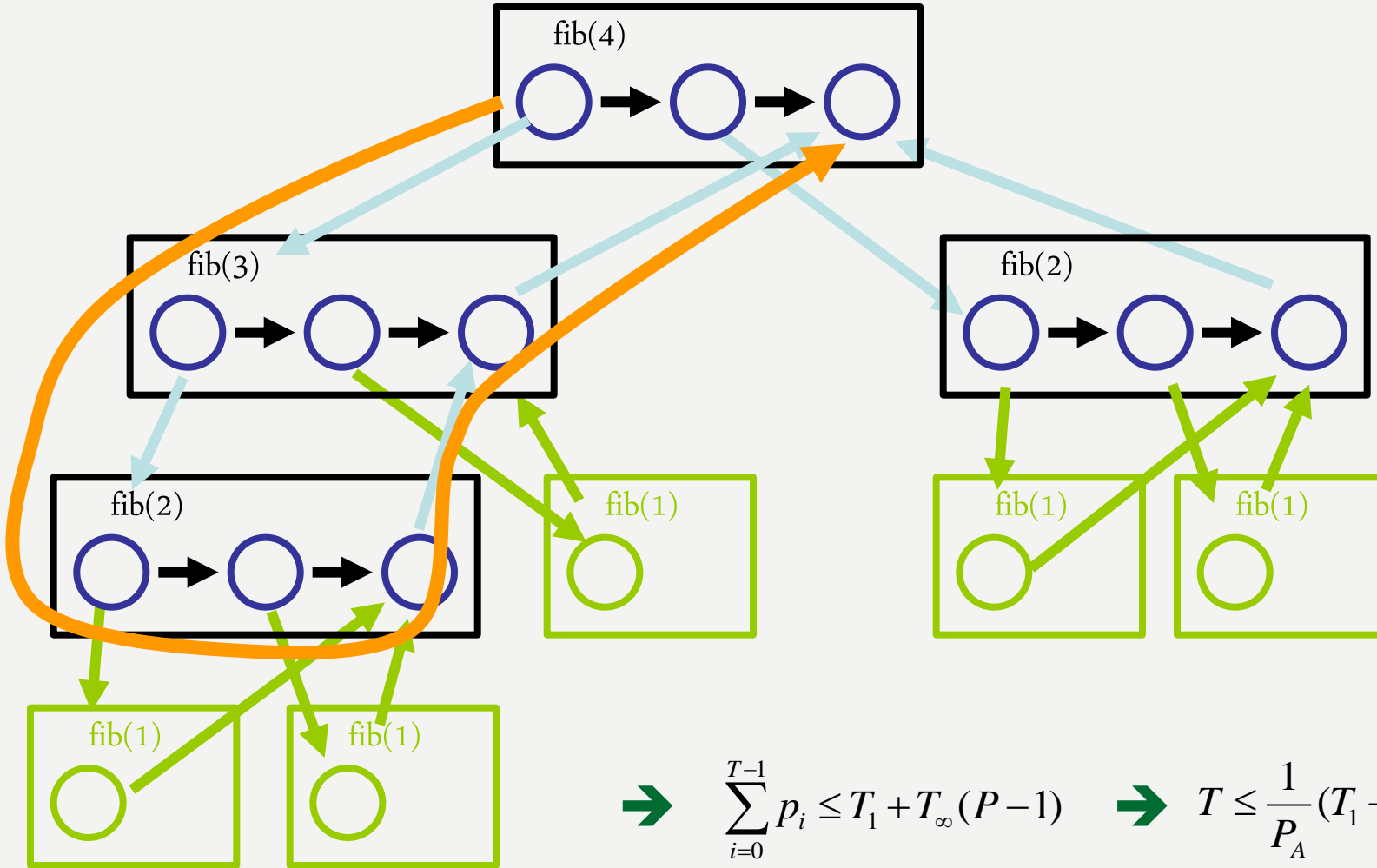
Realistic Multiprocessor Scheduling

- Internes 3-Level-Model: User Level / Scheduler / Kernel Level
- kein Zugriff auf Kernel Level
 - > Kein P Speedup möglich, aber:

> Pa Speedup:
$$P_A = \frac{1}{T} \sum_{i=0}^{T-1} p_i \qquad T = \frac{1}{P_A} \sum_{i=0}^{T-1} p_i$$

- Theorem zur maximale Steplänge(T) in einem Multithread Programm:

$$\frac{T_1}{P_A} + \frac{T_\infty(P-1)}{P_A}$$



$$\Rightarrow \sum_{i=0}^{T-1} p_i \leq T_1 + T_\infty (P-1) \quad \Rightarrow \quad T \leq \frac{1}{P_A} (T_1 + T_\infty (P-1))$$



Work Distribution

- Work Dealing: Beschäftigte Threads geben Arbeit an unbeschäftigte ab - ineffektiv
- Konsequenz: Work-Stealing – Threads ohne Tasks holen sich Arbeit von anderen
- Jeder Thread besitzt einen Pool an Tasks die in Form einer DEQueue (Double-Ended-Queue) gespeichert werden.
Diese stellt zum Zugriff die vier Methoden Push/Pop-Top/Bottom() zur Verfügung.



```
1 public class WorkStealingThread {
2     DEQueue[] queue;
3     int me;
4     Random random;
5     public WorkStealingThread(DEQueue[] myQueue) {
6         queue = myQueue;
7         random = new Random();
8     }
9     public void run() {
10        int me = ThreadID.get();
11        Runnable task = queue[me].popBottom();
12        while(true) {
13            while (task != null) {
14                task.run();
15                task = queue[me].popBottom();
16            }
17            while (task == null) {
18                Thread.yield();
19                int victim = random.nextInt(queue.length);
20                if (!queue[victim].isEmpty()) {
21                    task = queue[victim].popTop();
22                }
23            }
24        }
25    }
26 }
```



Bounded Work-Stealing DEQueue

```
1 public class BDEQueue {
2     Runnable[] tasks;
3     volatile int bottom;
4     AtomicStampedReference<Integer> top;
5     public BDEQueue(int capacity) {
6         tasks = new Runnable[capacity];
7         top = new AtomicStampedReference<Integer>(0, 0);
8         bottom = 0;
9     }
10    public void pushBottom(Runnable r) {
11        tasks[bottom] = r;
12        bottom++;
13    }
14    boolean isEmpty() {
15        return (top.getReference() < bottom);
16    }
17 }
```



Bounded Work-Stealing DEQueue

```
1 public Runnable popTop() {
2     int[] stamp = new int[1];
3     int oldTop = top.get(stamp), newTop = oldTop + 1;
4     int oldStamp = stamp[0], newStamp = oldStamp + 1;
5     if (bottom <= oldTop)
6         return null;
7     Runnable r = tasks[oldTop];
8     if (top.compareAndSet(oldTop, newTop, oldStamp, newStamp))
9         return r;
10    return null;
11 }
```

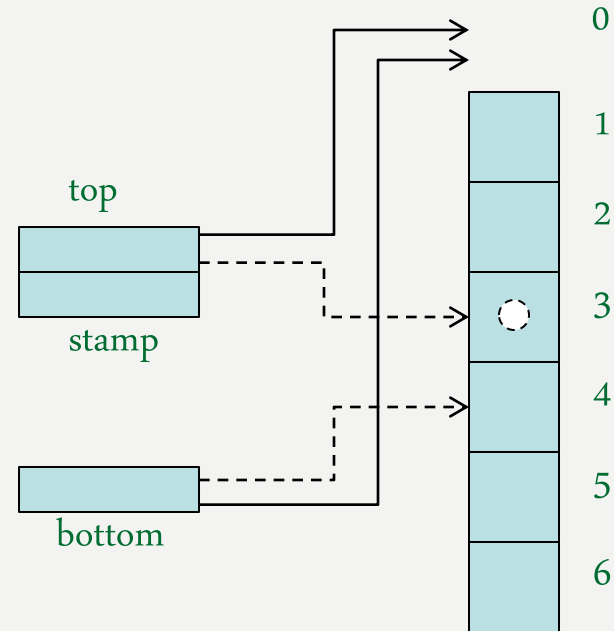
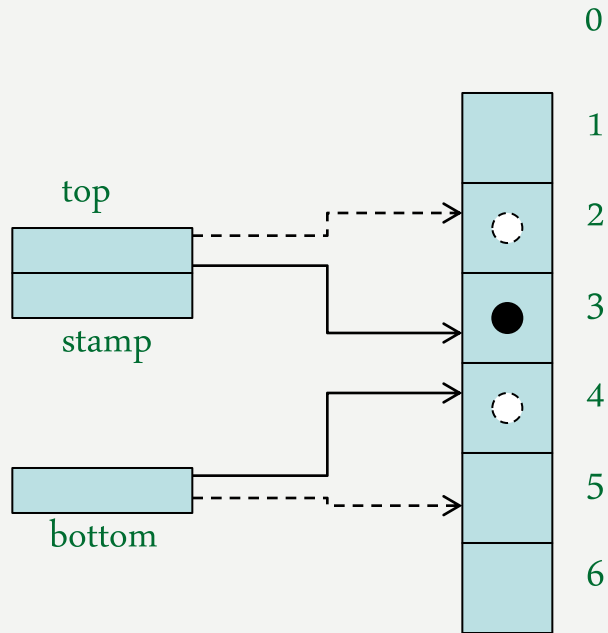


Bounded Work-Stealing DEQueue

```
12 public Runnable popBottom() {
13     if (bottom == 0)
14         return null;
15     bottom--;
16     Runnable r = tasks[bottom];
17     int[] stamp = new int[1]
18     int oldTop = top.get(stamp), newTop = 0;
19     int oldStamp = stamp[0], newStamp = oldStamp + 1;
20     if (bottom > oldTop)
21         return r;
22     if (bottom == oldTop) {
23         bottom = 0;
24         if (top.compareAndSet(oldTop, newTop, oldStamp, newStamp))
25             return r;
26     }
27     top.set(newTop, newStamp);
28     return null;
29 }
```




Bounded Work-Stealing DEQueue





Bounded Work-Stealing DEQueue

- push/pop – Methoden um Tasks aus einer DEQueue zu holen oder hinzuzufügen
 - yield – Methode um Prozessoren effektiv an arbeitende Threads zu verteilen
 - stamps um ABA Problem zu lösen und Mehrfachzugriffe zu vermeiden
 - compareAndSet wird erst aufgerufen wenn eine DEQueue sehr klein wird um Prozessorlast zu sparen
 - bottom Variable wird volatile deklariert, damit Arbeit suchende Threads gleich informiert werden wenn ein anderer Thread leer ist (da bottom nicht synchronized/atomic ist)
- ➔ Problem: Nicht für Threads geeignet die zufällig sehr viel oder wenig Arbeit haben
- ➔ Lösung: Unbounded Work-Stealing DEQueues



```
1  class CircularArray {
2      private int logCapacity;
3      private Runnable[] currentTasks;
4      CircularArray(int myLogCapacity) {
5          logCapacity = myLogCapacity;
6          currentTasks = new Runnable[1 << logCapacity];
7      }
8      int capacity() {
9          return 1 << logCapacity;
10     }
11     Runnable get(int i) {
12         return currentTasks[i % capacity()];
13     }
14     void put(int i, Runnable task) {
15         currentTasks[i % capacity()] = task;
16     }
17     CircularArray resize(int bottom, int top) {
18         CircularArray newTasks = new CircularArray(logCapacity+1);
19         for (int i = top; i < bottom; i++) {
20             newTasks.put(i, get(i));
21         }
22         return newTasks;
23     }
24 }
```



```
1  public class UnboundedDEQueue {
2      private final static int LOG_CAPACITY = 4;
3      private volatile CircularArray tasks;
4      volatile int bottom;
5      AtomicReference<Integer> top;
6      public UnboundedDEQueue(int LOG_CAPACITY) {
7          tasks = new CircularArray(LOG_CAPACITY);
8          top = new AtomicReference<Integer>(0);
9          bottom = 0;
10     }
11     boolean isEmpty() {
12         int localTop = top.get();
13         int localBottom = bottom;
14         return (localBottom <= localTop);
15     }
16
17     public void pushBottom(Runnable r) {
18         int oldBottom = bottom;
19         int oldTop = top.get();
20         CircularArray currentTasks = tasks;
21         int size = oldBottom - oldTop;
22         if (size >= currentTasks.capacity() - 1) {
23             currentTasks = currentTasks.resize(oldBottom, oldTop);
24             tasks = currentTasks;
25         }
26         tasks.put(oldBottom, r);
27         bottom = oldBottom + 1;
28     }
}
```



Unbounded Work-Stealing DEQueue

```
30 public Runnable popTop() {
31     int oldTop = top.get();
32     int newTop = oldTop + 1;
33     int oldBottom = bottom;
34     CircularArray currentTasks = tasks;
35     int size = oldBottom - oldTop;
36     if (size <= 0) return null;
37     Runnable r = tasks.get(oldTop);
38     if (top.compareAndSet(oldTop, newTop))
39         return r;
40     return null;
41 }
```

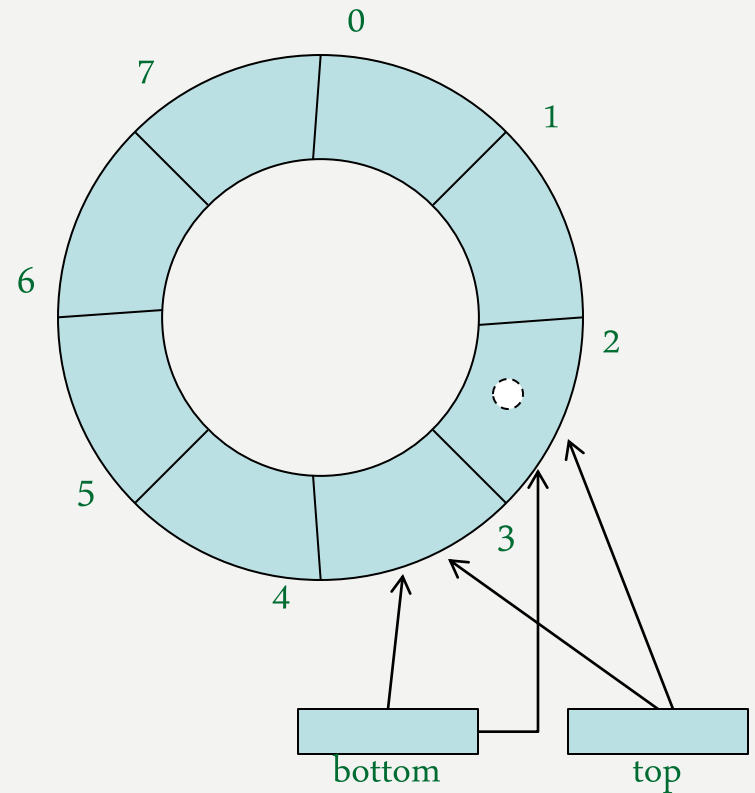
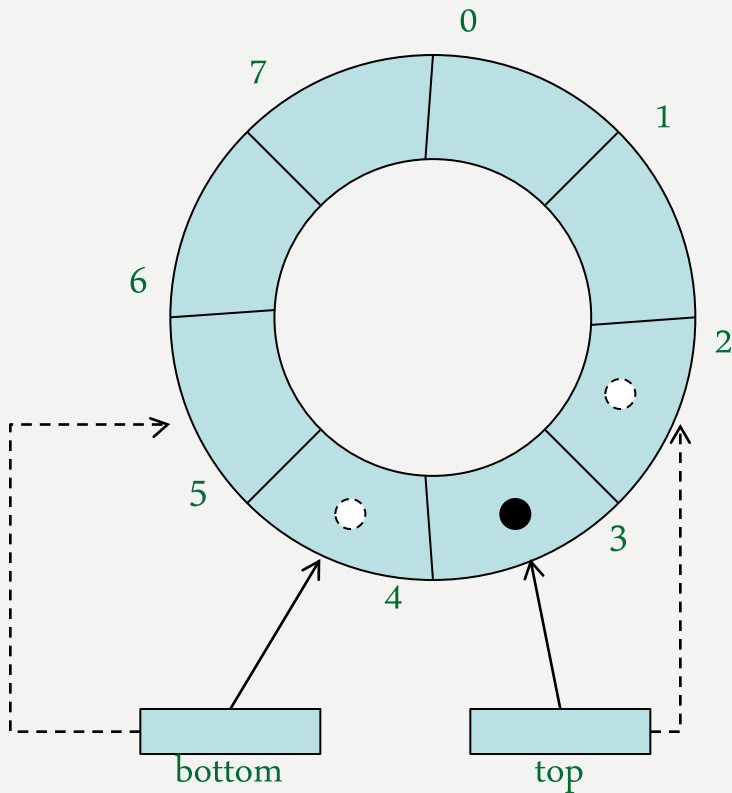


Unbounded Work-Stealing DEQueue

```
43 public Runnable popBottom() {
44     CircularArray currentTasks = tasks;
45     bottom--;
46     int oldTop = top.get();
47     int newTop = oldTop + 1;
48     int size = bottom - oldTop;
49     if (size < 0) {
50         bottom = oldTop;
51         return null;
52     }
53     Runnable r = tasks.get(bottom);
54     if (size > 0)
55         return r;
56     if (!top.compareAndSet(oldTop, newTop))
57         r = null;
58     bottom = oldTop + 1;
59     return r;
60 }
```



Unbounded Work-Stealing DEQueue





Unbounded Work-Stealing DEQueue

- Kreis Array um einen Reset von bottom und top auf 0 zu vermeiden und um Grösse dynamisch erweitern zu können
- Kreis Array ermöglicht weiterhin, dass top nur inkrementiert wird und verzichtet deshalb auf eine AtomicStampedReference
- pushBottom Methode vergrößert das Array dynamisch
- beim Kopieren in ein neues Array müssen top und bottom nie angepasst werden, da das Array immer mit $\text{Index mod Kapazität}$ angelegt wird



Work Balancing

- Alternativer Ansatz zum Verteilen von Tasks aufs Threads:
 - > Threads gleichen regelmäßig ihren Workload mit Nachbar Threads aus
- Um Prozessorlast zu vermeiden initialisieren nur weniger ausgelastete Threads den Ausgleich
- Die Wahrscheinlichkeit zum Ausgleich ist entsprechend invers-proportional zur Taskmenge
- Vorteil: Mehrere Tasks werden gleichzeitig in einen anderen geschoben



```
1 public class WorkSharingThread {
2     Queue[] queue;
3     Random random;
4     private static final int THRESHOLD = ...;
5     public WorkSharingThread(Queue[] myQueue) {
6         queue = myQueue;
7         random = new Random();
8     }
9     public void run() {
10        int me = ThreadID.get();
11        while(true) {
12            Runnable task = queue[me].deq();
13            if (task != null) task.run();
14            int size = queue[me].size();
15            if (random.nextInt(size+1) == size) {
16                int victim = random.nextInt(queue.length);
17                int min = (victim <= me) ? victim : me;
18                int max = (victim <= me) ? me : victim;
19                synchronized (queue[min]) {
20                    synchronized (queue[max]) {
21                        balance(queue[min], queue[max]);
22                    }
23                }
24            }
25        }
26    }
27 }
```



Work Balancing

```
27 private void balance(Queue q0, Queue q1) {
28     Queue qMin = (q0.size() < q1.size()) ? q0 : q1;
29     Queue qMax = (q0.size() < q1.size()) ? q1 : q0;
30     int diff = qMax.size() - qMin.size();
31     if (diff > THRESHOLD)
32         while (qMax.size() > qMin.size())
33             qMin.enq(qMax.deq());
34 }
35 }
```



Quellen:

- M. Herlihy and N. Shavit. **The art of multiprocessor programming. 2008, Morgan Kaufmann Publishers.**
- <http://www.elsevierdirect.com/companion.jsp?ISBN=9780123705914>